

# VIB : MDOF systems

Number of participants: 34

**1. Would you to skip the break and end a bit earlier** **0 correct answer**  
out of 18 respondents

No, I still prefer a 10minute break at 15:00 17% 3 votes

Yes, I prefer to end a bit earlier 83% 15 votes

**2. (Exercises) Type your name if you are still not able to login on Canvas.** 2 respondents

SALLEYRETTE Mathieu

Léon

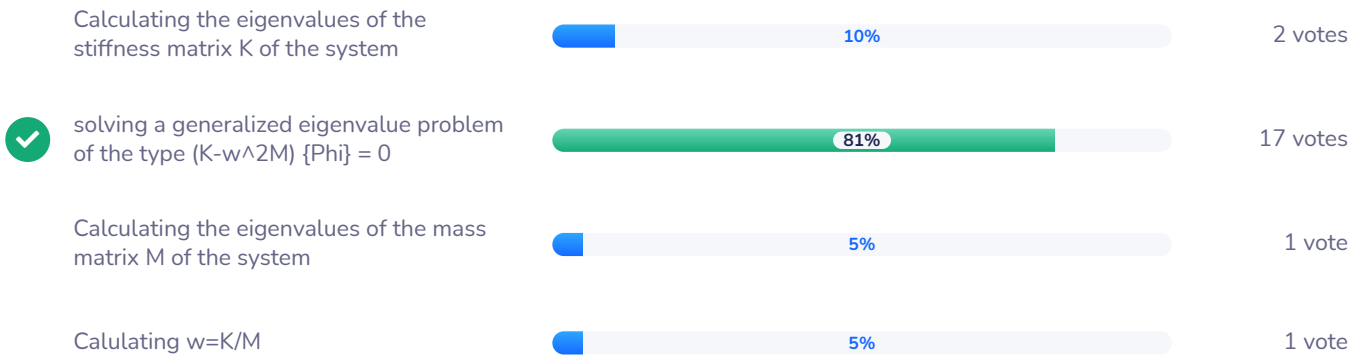
**3. Who watched the video on MDOF systems?** **0 correct answer**  
out of 20 respondents

Yes 50% 10 votes

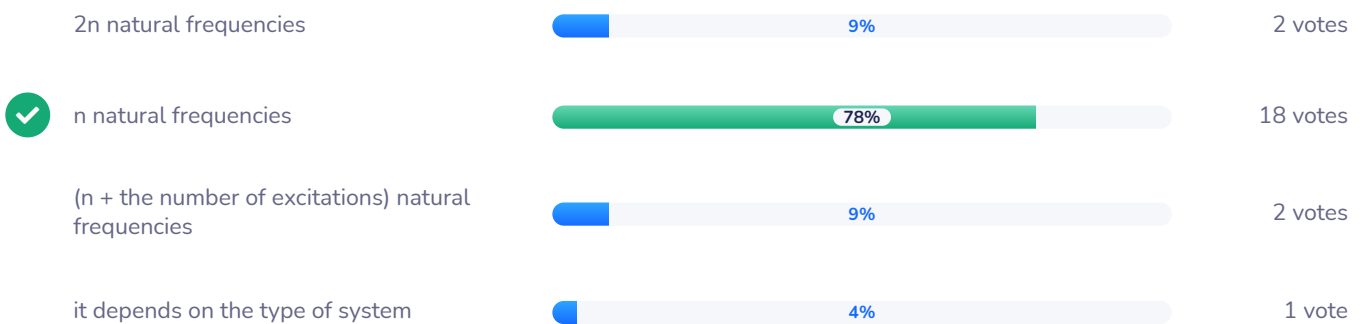
Yes, but at 1.5x speed 40% 8 votes

No 10% 2 votes

**4. The mode shapes and eigenfrequencies of a system are determined by (K and M are the stiffness and mass matrices)** **17 correct answers**  
out of 21 respondents

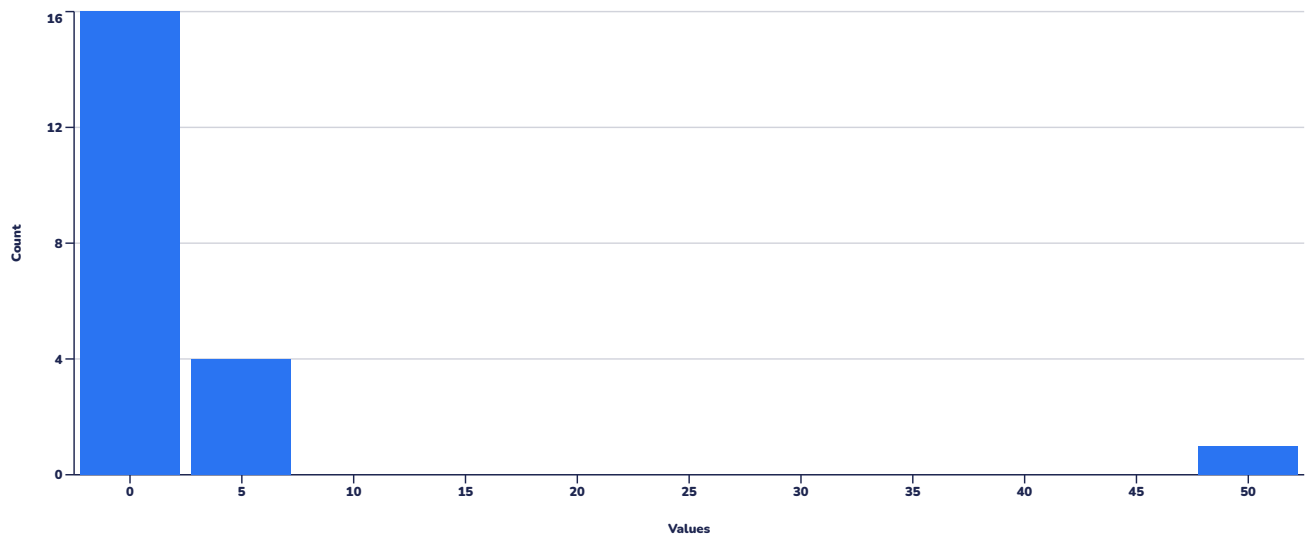


**5. If a system has n degrees of freedom, it has** **18 correct answers**  
out of 23 respondents



6. How many Degrees of freedom would this real world structure have?

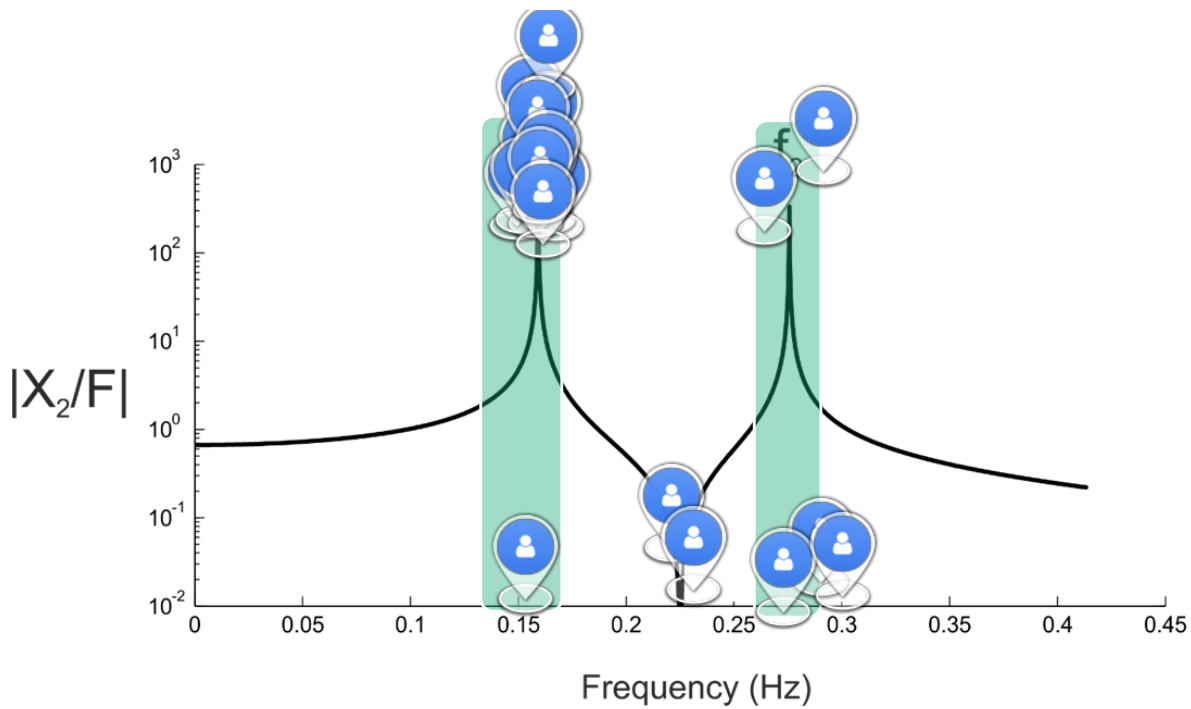
21 respondents



<b>1</b> Minimum	<b>5.1</b> Mean	<b>50</b> Maximum	<b>2</b> Median	<b>10.28</b> Standard deviation	<b>105.61</b> Variance
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**7. Where are the resonant frequencies of the 2 DOFs system on this graph ?**

24 respondents



19

**8. The mode shapes are orthogonal with respect to the**

**12 correct answers**  
out of 28 respondents

- stiffness matrix 82% 23 votes
- mass matrix 54% 15 votes
- damping matrix 14% 4 votes

**9. The interest of projecting the equations of motion in the modal domain is to:**

**19 correct answers**  
out of 25 respondents

- reduce the number of equations to solve 12% 3 votes
- decouple the equations of motion and facilitate solving them 76% 19 votes
- work with physical quantities for a better understanding of the system's behavior 12% 3 votes

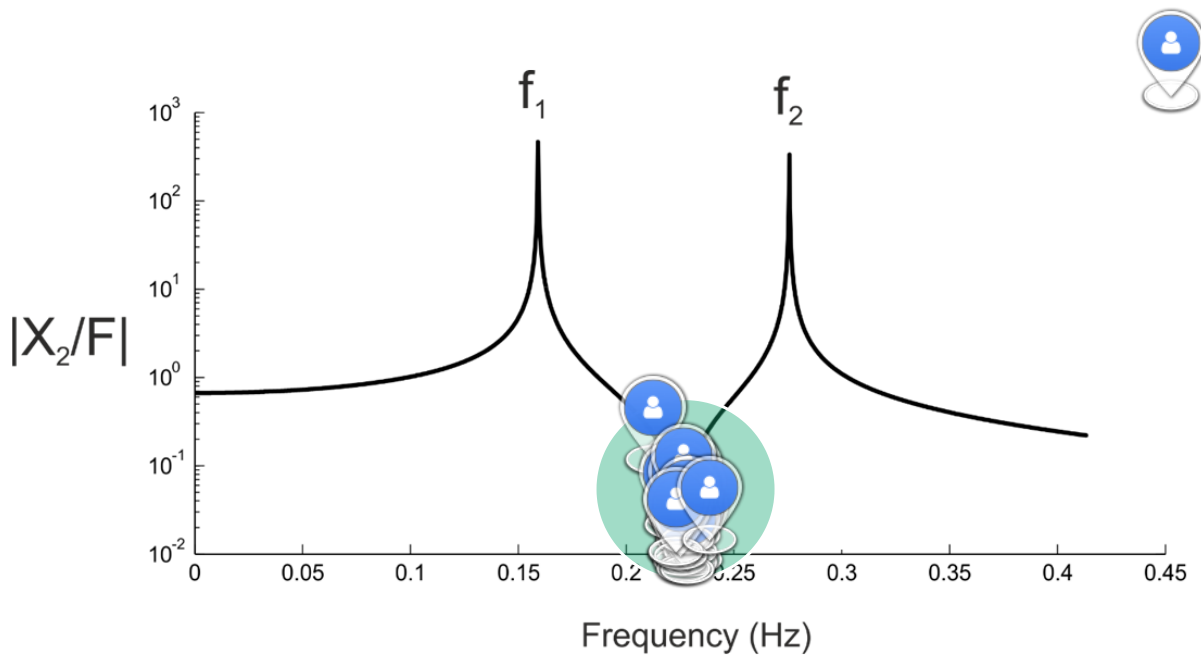
**10. Which of these quantities is a global quantity for a given structure**

**2 correct answers**  
out of 21 respondents

- the eigenfrequency 71% 15 votes
- the anti-resonance frequency 43% 9 votes
- the damping coefficient 19% 4 votes

**11. Where is the anti-resonance of the 2 DOFs system on this graph ?**

26 respondents



19

**12. An anti-resonance happens when**

**20 correct answers**  
out of 27 respondents

- The contribution to the response of the two close modes as equal amplitude and equal phase 15% 4 votes
- The contribution to the response of the two close modes has equal amplitude and opposite phase 74% 20 votes
- The displacement is zero for the two closest modes 11% 3 votes

**13. Complete following statement about anti-resonances for a 2DOF system (X1,X2)?**

5 respondents

When X2 has an anti-resonance at frequency  $f_0$  it will not displace when excited by a(n) **harmonic** (4) force with a frequency **equal to  $f_0$**  (0) and X1 **will** (4) displace.

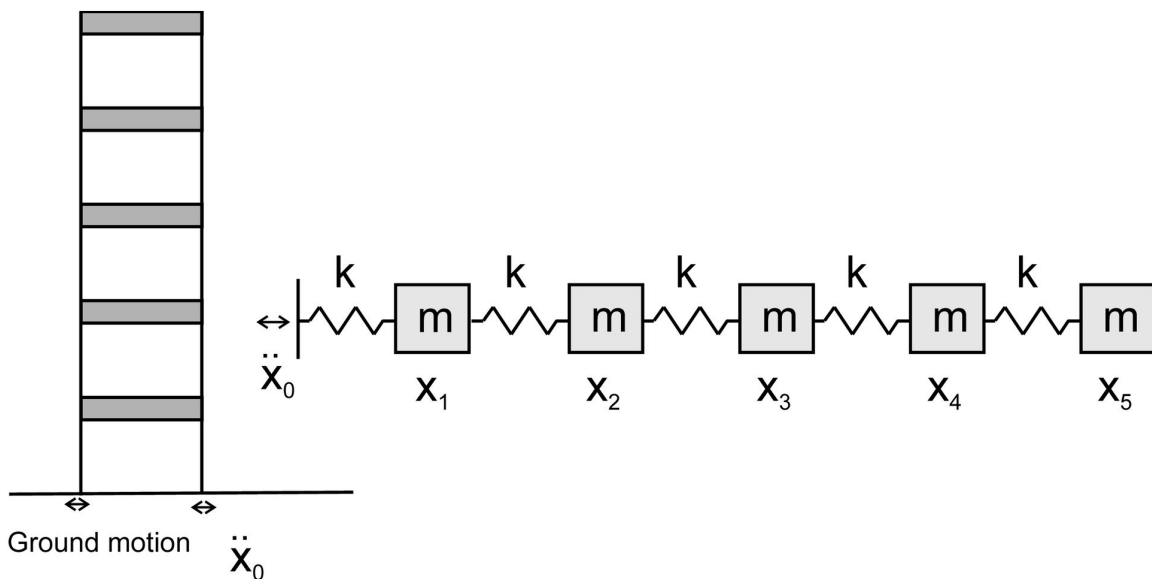
**14. What kind of hypothesis can be made on the damping matrix to decouple the equations of motion in the modal domain ?**

8 correct answers out of 21 respondents

- Rayleigh Damping 71% 15 votes
- Lagrange Damping 19% 4 votes
- Modal damping 43% 9 votes
- Viscous damping 5% 1 vote

**15. How many mode shapes and eigenfrequencies does this building simplified model have ?**

13 correct answers out of 15 respondents



- one 0% 0 votes
- three 0% 0 votes
- five 87% 13 votes
- an infinity 13% 2 votes

**16. If this system is excited with an harmonic force applied to the bottom mass, whose frequency is close to the first natural frequency, the motion will correspond to**

**8 correct answers**  
out of 21 respondents

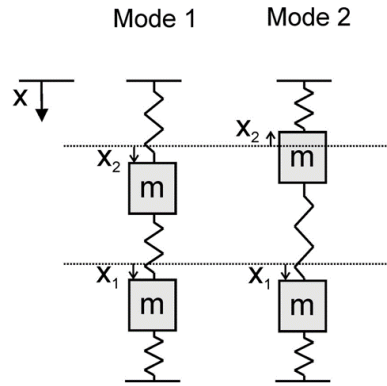
**2 DOFs system mode shapes**

$$\omega_1^2 = k/m$$

$$\psi_1 = \begin{Bmatrix} 1 \\ 1 \end{Bmatrix}$$

$$\omega_2^2 = 3k/m$$

$$\psi_2 = \begin{Bmatrix} 1 \\ -1 \end{Bmatrix}$$



14



The first mode shape where the two masses move in phase



38%

8 votes

The second mode shape where the two masses move out of phase



10%

2 votes

A combination of the two modeshapes



52%

11 votes



17.

If this system is excited with an harmonic force applied to the bottom mass, whose frequency is the average of the first and second natural frequencies of the system, the motion will correspond to

22 correct answers  
out of 26 respondents

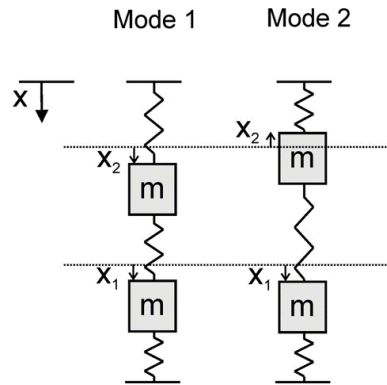
2 DOFs system mode shapes

$$\omega_1^2 = k/m$$

$$\psi_1 = \begin{Bmatrix} 1 \\ 1 \end{Bmatrix}$$

$$\omega_2^2 = 3k/m$$

$$\psi_2 = \begin{Bmatrix} 1 \\ -1 \end{Bmatrix}$$



14

The first mode shape where the two masses move in phase



0 votes

The second mode shape where the two masses move out of phase



4 votes



A combination of the two mode shapes



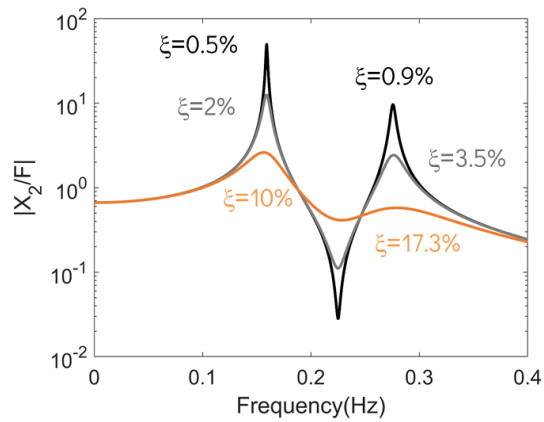
22 votes



18. Why is the damping coefficient higher for the second mode than for the first mode for the damped two dofs system treated in the examples of the course ?

4 respondents

### Example of a 2 DOFs system



$k=1 \text{ N/m}$ ,  $m=1\text{kg}$ ,

$b=0.01 \text{ N/ms}$

$b=0.04 \text{ N/ms}$

$b=0.2 \text{ N/ms}$

37

The  $x_2$  value in the  $\omega_{n2}$  frequency is lower than in  $\omega_{n1}$

Sqrt3

Because  $\sqrt{3}$

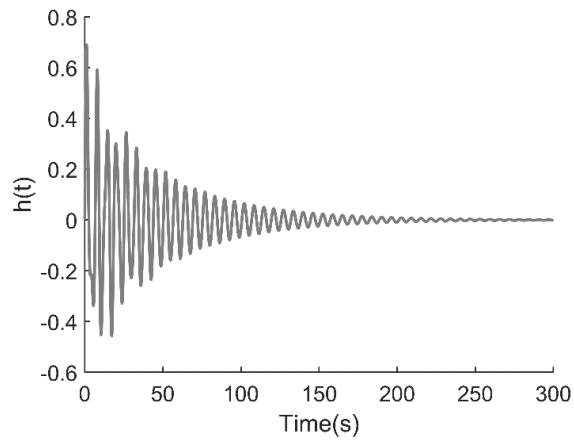
There are more damping points affecting the second mode



19. **This is the impulse response of a damped two dofs system. Is it possible to extract the information on the first natural frequency and damping from this curve in a simple way ?**

12 correct answers  
out of 23 respondents

### Impulse response



40



Yes

52%

12 votes

No

48%

11 votes



20. **How would you extract the first natural frequency from the impulse response ?**

0 respondent

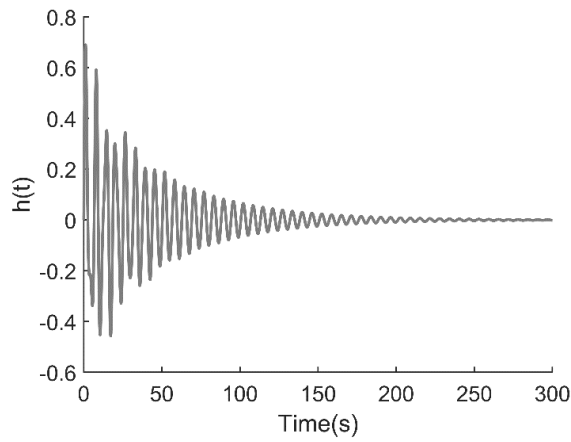
No answers in this question



**21. This is the impulse response of a damped two dofs system. Is it possible to extract the information on the second natural frequency and damping from this curve ?**

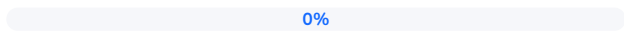
22 correct answers  
out of 23 respondents

**Impulse response**



40

Yes, you can see the response of the second mode very clearly.



0 votes



Yes, while you might not see it well, all information on the second mode is also contained in this response



22 votes

No, impulse responses show only the response from one mode at a time



1 vote

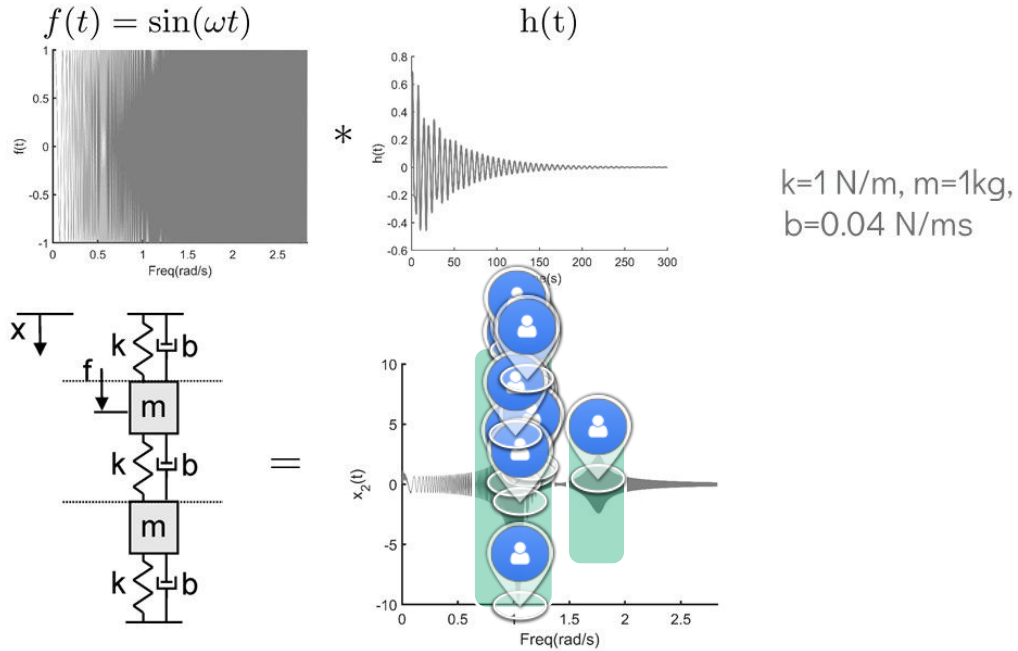
**This is the time domain response of a damped 2 DOFs**



**22. system under sine sweep excitation. Where do you see the resonances on the time domain response ?**

15 respondents

## Sine sweep excitation



50



**23. When a system is excited by its base, it is easier to write the unknown displacements**

**12 correct answers**  
out of 24 respondents

as relative displacement between the neighbouring DOFS



10 votes



as relative displacement between the base and each DOF.



12 votes

in mm instead of m



2 votes



**24. When doing so, the equation of motion is equivalent to the case of an applied force which is**

**12 correct answers**  
out of 19 respondents



proportional to the applied acceleration



12 votes

inversely proportional to the applied acceleration



3 votes

proportional to the applied displacement



4 votes